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# **Self-Organizing Recurrent Neural Network (SORN)**

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# GETTING STARTED

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Self-Organizing Recurrent Neural (SORN) networks are a class of reservoir computing models build based on plasticity mechanisms in biological brain. Recent studies on SORN shows that such models can mimic neocortical circuit's ability of learning and adaptation through neuroplasticity mechanisms. Structurally, unlike other liquid state models, SORN consists of pool of excitatory neurons and small population of inhibitory neurons. First such network was introduced with three fundamental plasticity mechanisms found in neocortex, namely Spike timing dependent plasticity (STDP), intrinsic plasticity (IP) and Synaptic scaling (SS). Spike Timing-Dependent Plasticity or Hebbian Learning with positive feedback (rapid cycle of synaptic potentials) selectively strengthens correlated synapses and weaken the uncorrelated. Such activity dependent rules lead to Long Time Potentiation (LTP) and Long Time Depression (LTD).

Biologically, both LTP and LDP are assumed to possess substrates of learning and memory at the cellular level of neocortex. However, in dynamical systems, such phenomena will drive the network either towards the state of bursting activity in case of LTP or towards state of attenuation due to LTD. These destabilizing influences of STDP are counteracted by homeostatic plasticity mechanisms. Homeostatic mechanisms are a set of negative feedback (action potential suppressing) regulatory mechanisms that scales incoming synaptic strengths and balances neuronal activity through synaptic normalization and intrinsic plasticity. Experimental evidences also prove that synaptic scaling found to balance the activity between excitatory and inhibitory neurons in-vivo. Together, they maintain the overall activity of network within subcritical range, despite the network being driven by positive feedback from fast Hebbian plasticity.

In recent proposed models, SORN is extended with two more plasticity mechanisms, inhibitory spike timing dependent plasticity and structural plasticity. While connections between excitatory neurons (E-E) subjected to STDP rules, connections from inhibitory population to excitatory populations(E-I) are regulated by iSTDP. Structural plasticity, generates new connections constantly at a smaller rate between unconnected synapses. Many studies argued that, such structural changes induce neuronal morphogenesis which leads to network re-organization with functional consequences over learning and memory. The mathematical descriptions of plasticity mechanisms proposed in SORN simplifies the structural and functional connectivity mechanisms that resembles information processing, learning and memory phenomena that occur in neuro-synapses of neocortex region. Recent experimental evidences confirm that SORN outperforms other static reservoir networks in spatio-temporal tasks and maintains the dynamics of the network in subcritical state suitable for learning. Further research on such network mechanisms unravels the underlying features of synaptic connections and network activity in real cortical circuits. Hence investigating the characteristics of SORN and extending its structural and functional attributes by replicating the recent findings in neural connectomics may reveal the dominating principles of self-organization and self-adaptation in neocortical circuits at microscopic level. Moreover, characterizing these mechanisms individually at that level may also help us to understand some fundamental aspects of brain networks at mesoscopic and macroscopic scales.



## INSTALLATION

Install using *pip*

```
pip install sorn
```

or

To install the latest version from the development branch

```
pip install git+https://github.com/Saran-nns/sorn
```

### 1.1 Dependencies

SORN supports Python 3.5+ ONLY. For older Python versions please use the official Python client

To install all optional dependencies run

```
pip install 'sorn[all]'
```



## 2.1 Plasticity Phase

```
import sorn
from sorn import Simulator
import numpy as np

# Sample input
num_features = 10
time_steps = 200
inputs = np.random.rand(num_features, time_steps)

# Simulate the network with default hyperparameters under gaussian white noise
state_dict, E, I, R, C = Simulator.simulate_sorn(inputs = inputs, phase='plasticity',
                                                  matrices=None, noise = True,
                                                  time_steps=time_steps)
```

```
Network Initialized
Number of connections in Wee 3909 , Wei 1574, Wie 8000
Shapes Wee (200, 200) Wei (40, 200) Wie (200, 40)
```

The default values of the network hyperparameters are,

Table 1: Hyperparameters of the network and default values

Keyword argument	Value	Description
ne	200	Number of Encitatory neurons in the reservoir
nu	10	Number of Input neurons in the reservoir
network_type_ee	“Sparse”	<i>Sparse</i> or <i>Dense</i> connectivity between Excitatory neurons
network_type_ie	“Dense”	<i>Sparse</i> or <i>Dense</i> connectivity from Excitatory to Inhibitory neurons
network_type_ei	“Sparse”	<i>Sparse</i> or <i>Dense</i> connectivity from Inhibitory to Excitatory neurons
lambda_ee	20	% of connections between neurons in Excitatory pool
lambda_ei	40	% of connections from Inhibitory to Excitatory neurons
lambda_ie	100	% of connections from Excitatory to Inhibitory neurons
eta_stdp	0.004	Hebbian Learning rate for connections between excitatory neurons
eta_inhib	0.001	Hebbian Learning rate for connections from Inhibitory to Excitatory neurons
eta_ip	0.01	Intrinsic plasticity learning rate
te_max	1.0	Maximum excitatory neuron threshold value
ti_max	0.5	Maximum inhibitory neuron threshold value
ti_min	0.0	Minimum inhibitory neuron threshold value
te_min	0.0	Minimum excitatory neuron threshold value
mu_ip	0.01	Target mean firing rate of excitatory neuron
sigma_ip	0.0	Standard deviation of firing rate of excitatory neuron

## 2.1.1 Override the default hyperparameters and simulate new SORN model

```
# Sample input
num_features = 5
time_steps = 1000
inputs = np.random.rand(num_features,time_steps)

state_dict, E, I, R, C = Simulator.simulate_sorn(inputs = inputs, phase='plasticity',
                                                matrices=None, noise = True,
                                                time_steps=time_steps,
                                                ne = 100, nu=num_features,
                                                lambda_ee = 10, eta_stdp=0.001)
```

```
Network Initialized
Number of connections in Wee 959 , Wei 797, Wie 2000
Shapes Wee (100, 100) Wei (20, 100) Wie (100, 20)
```

## 2.2 Training phase

```

from sorn import Trainer
# NOTE: During training phase, input to `sorn` should have second (time) dimension set to 1. ie., input shape should be (input_features,1).

inputs = np.random.rand(num_features,1)

# SORN network is frozen during training phase
state_dict, E, I, R, C = Trainer.train_sorn(inputs = inputs, phase='training',
                                             matrices=state_dict, noise= False,
                                             time_steps=1,
                                             ne = 100, nu=num_features,
                                             lambda_ee = 10, eta_stdp=0.001 )

```

## 2.3 Freeze plasticity

To turn off any plasticity mechanisms during simulation or training phase, use freeze argument. For example to stop intrinsic plasticity during simulation phase,

```

# Sample input
num_features = 10
time_steps = 20
inputs = np.random.rand(num_features,time_steps)

state_dict, E, I, R, C = Simulator.simulate_sorn(inputs = inputs, phase='plasticity',
                                                  matrices=None, noise = True,
                                                  time_steps=time_steps, ne = 50,
                                                  nu=num_features, freeze=['ip'])

```

To train the above model under plasticity mechanisms except ip and istdp, use freeze argument

```

state_dict, E, I, R, C = Trainer.train_sorn(inputs = inputs, phase='plasticity',
                                             matrices=state_dict, noise= False,
                                             time_steps=1,
                                             ne = 50, nu=num_features,
                                             freeze=['ip','istdp'])

```

To train the above model with all plasticity mechanisms frozen , change the phase argument value to training

```

state_dict, E, I, R, C = Trainer.train_sorn(inputs = inputs, phase='training',
                                             matrices=state_dict, noise= False,
                                             time_steps=1,
                                             ne = 50, nu=num_features)

```

The other options are,

*stdp* - Spike Timing Dependent Plasticity

*ss* - Synaptic Scaling

*sp* - Structural Plasticity

*istdp* - Inhibitory Spike Timing Dependent Plasticity

Note: If you pass all above options to freeze, then the network will behave as Liquid State Machine(LSM) i.e., the connection strengths and thresholds remains fixed at the random initial state.

## 2.4 Network Output Descriptions

*state\_dict* - Dictionary of connection weights (*Wee*, *Wei*, *Wie*),

Excitatory network activity (*X*),

Inhibitory network activities(*Y*),

Threshold values (*Te*, *Ti*)

*E* - Excitatory network activity of entire simulation period

*I* - Inhibitory network activity of entire simulation period

*R* - Recurrent network activity of entire simulation period

*C* - Number of active connections in the Excitatory pool at each time step

## 2.5 Colaboratory Notebook

Sample simulation and training runs with few plotting functions are found at Colab

## 2.6 Usage with OpenAI gym

### 2.6.1 Cartpole balance problem

```
from sorn import Simulator, Trainer
import gym

# Hyperparameters
NUM_EPISODES = int(2e6)
NUM_PLASTICITY_EPISODES = 20

LEARNING_RATE = 0.0001 # Gradient ascent learning rate
GAMMA = 0.99 # Discounting factor for the Rewards

# Open AI gym; Cartpole Environment
env = gym.make('CartPole-v0')
action_space = env.action_space.n

# SORN network parameters
ne = 50
nu = 4
# Init SORN using Simulator under random input;
state_dict, E, I, R, C = Simulator.simulate_sorn(inputs = np.random.randn(4,1),
                                                phase='plasticity',
                                                time_steps = 1,
                                                noise=False,
```

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```

ne = ne, nu=nu)

w = np.random.rand(ne, 2) # Output layer weights

# Policy
def policy(state,w):
    "Implementation of softmax policy"
    z = state.dot(w)
    exp = np.exp(z)
    return exp/np.sum(exp)

# Vectorized softmax Jacobian
def softmax_grad(softmax):
    s = softmax.reshape(-1,1)
    return np.diagflat(s) - np.dot(s, s.T)

for EPISODE in range(NUM_EPISODES):

    # Environment observation;
    # NOTE: Input to sorn should have time dimension. ie., input shape should be (input_
    ↪ features,time_steps)
    state = env.reset()[:, None] # (4,) --> (4,1)

    grads = [] # Episode log policy gradients
    rewards = [] # Episode rewards

    # Keep track of total score
    score = 0

    # Play the episode
    while True:

        # env.render() # Uncomment to see your model train in real time (slow down_
        ↪ training progress)
        if EPISODE < NUM_PLASTICITY_EPISODES:

            # Plasticity phase
            state_dict, E, I, R, C = Simulator.simulate_sorn(inputs = state, phase =
            ↪ 'plasticity',
                                                                matrices = state_dict, time_
            ↪ steps = 1,
                                                                ne = ne, nu=nu,
                                                                noise=False)

        else:
            # Training phase with frozen reservoir connectivity
            state_dict, E, I, R, C = Trainer.train_sorn(inputs = state, phase = 'training',
                                                                matrices = state_dict, time_steps = 1,
                                                                ne = ne, nu=nu,
                                                                noise= False)

        # Feed E as input states to your RL algorithm, below goes for simple policy_
        ↪ gradient algorithm

```

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```

# Sample policy w.r.t excitatory states and take action in the environment
probs = policy(np.asarray(E),w)
action = np.random.choice(action_space,p=probs[0])
state,reward,done,_ = env.step(action)
state = state[:,None]

# COMPUTE GRADIENTS BASED ON YOUR OBJECTIVE FUNCTION;
# Sample computation of policy gradient objective function
dsoftmax = softmax_grad(probs)[action,:]
dlog = dsoftmax / probs[0,action]
grad = np.asarray(E).T.dot(dlog[None,:])
grads.append(grad)
rewards.append(reward)
score+=reward

if done:
    break

# OPTIMIZE OUTPUT LAYER WEIGHTS `w` BASED ON YOUR OPTIMIZATION METHOD;
# Below is a sample of weight update based on gradient ascent(maximize cumulative_
↪reward) method for temporal difference learning
for i in range(len(grads)):

    # Loop through everything that happened in the episode and update towards the_
↪log policy gradient times future reward
    w += LEARNING_RATE * grads[i] * sum([ r * (GAMMA ** r) for t,r in_
↪enumerate(rewards[i:]))]
    print('Episode %s Score %s' %(str(EPISODE),str(score)))

```

There are several neural data analysis and visualization methods inbuilt with *sorn* package. Sample call for few plotting and statistical methods are shown below;

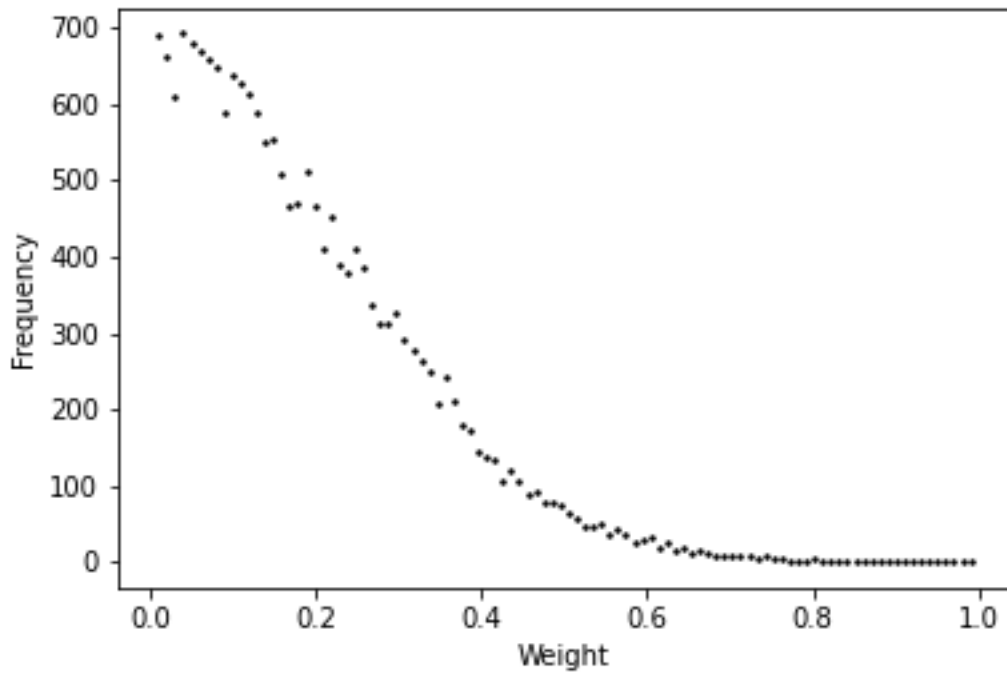
## 2.7 Plotting functions

### 2.7.1 Plot weight distribution in the network

```

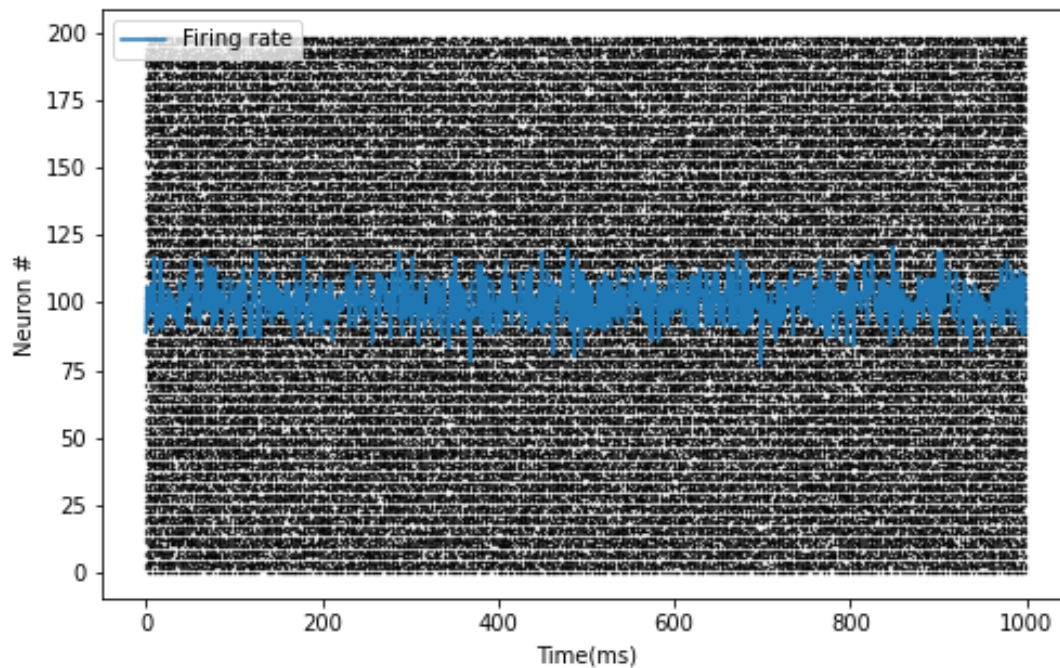
from sorn import Plotter
# For example, the network has 200 neurons in the excitatory pool.
Wee = np.random.randn(200,200) # Note that generally Wee is sparse
Wee=Wee/Wee.max() # state_dict['Wee'] returned by the SORN is already normalized
Plotter.weight_distribution(weights= Wee, bin_size = 5, savefig = True)

```



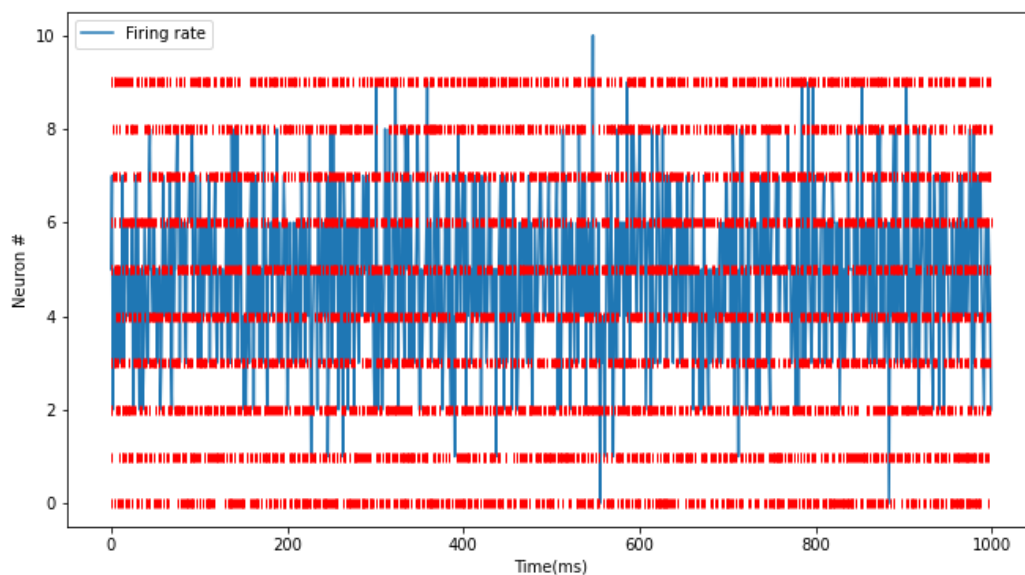
### 2.7.2 Plot Spike train

```
E = np.random.randint(2, size=(200,1000)) # For example, activity of 200 excitatory_
↳neurons in 1000 time steps
Plotter.scatter_plot(spike_train = E, savefig=True)
```



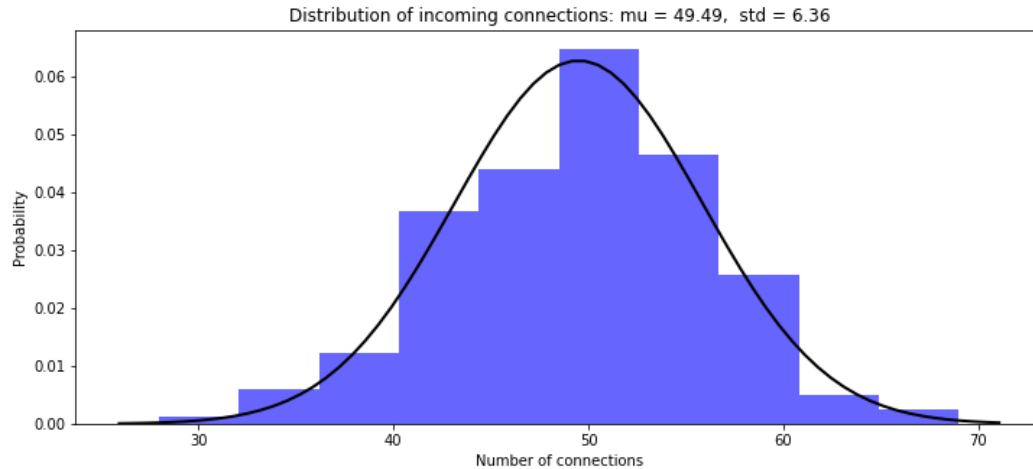
## 2.7.3 Raster plot of Spike train

# Raster plot of activity of only first 10 neurons in the excitatory pool  
`Plotter.raster_plot(spike_train = E[:,0:10], savefig=True)`



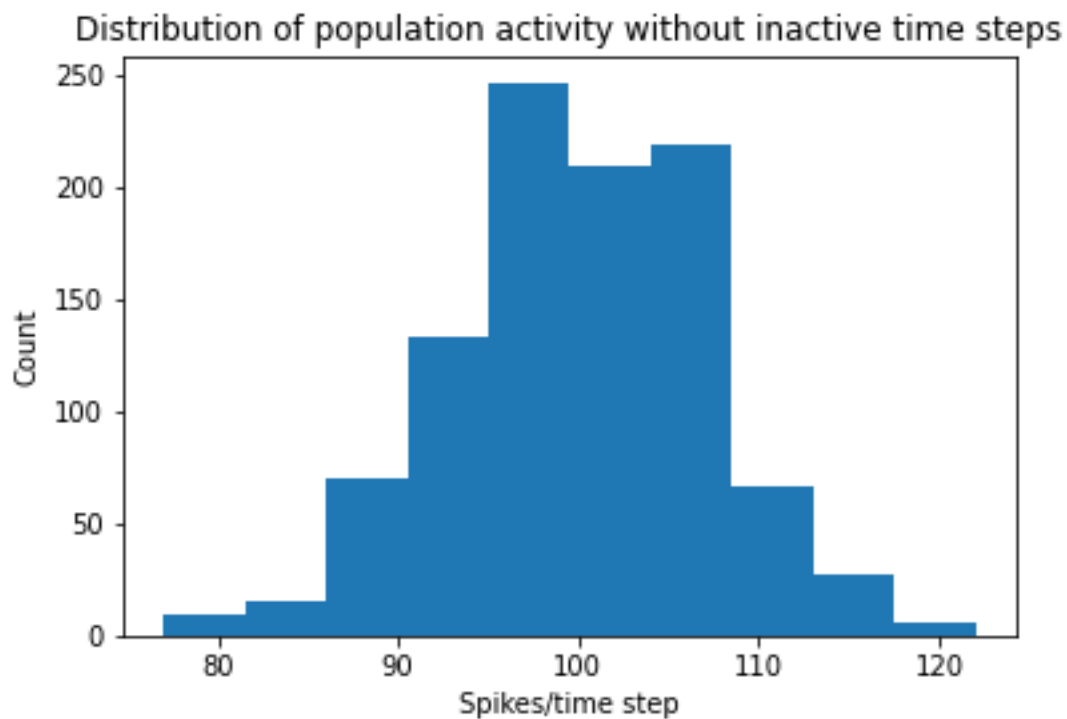
## 2.7.4 Distribution of presynaptic connections

```
# Histogram of number of presynaptic connections per neuron in the excitatory pool
Plotter.hist_incoming_conn(weights=Wee, bin_size=10, histtype='bar', savefig=True)
```



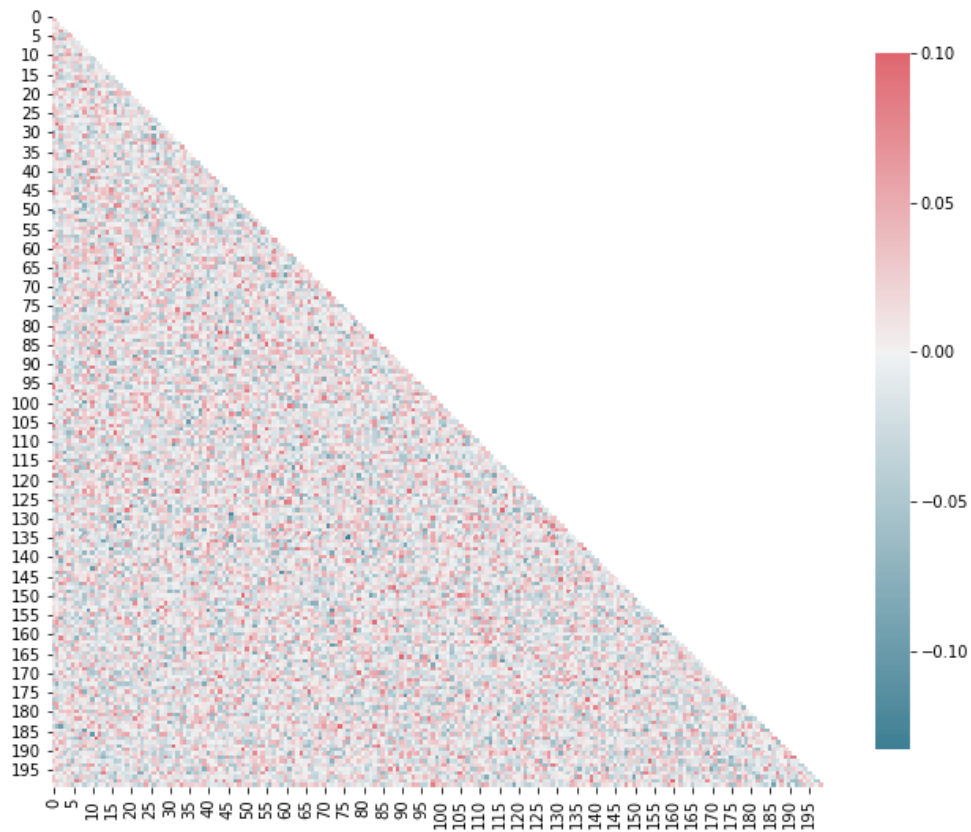
## 2.7.5 Distribution of firing rate of the network

```
Plotter.hist_firing_rate_network(E, bin_size=10, savefig=True)
```



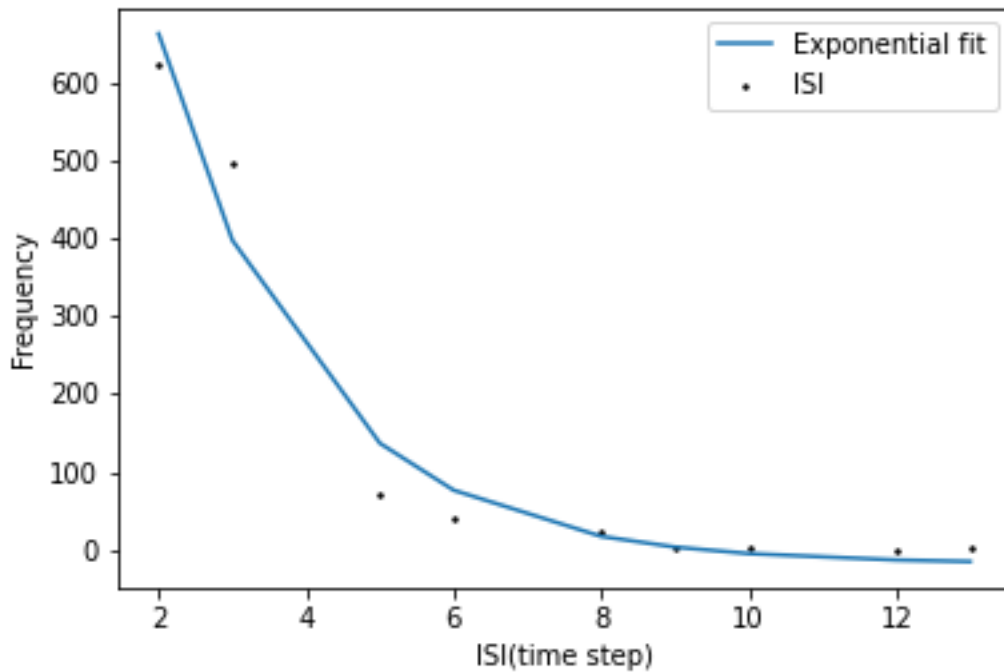
## 2.7.6 Plot pearson correlation between neurons

```
from sorn import Statistics
avg_corr_coeff,_ = Statistics.avg_corr_coeff(E)
Plotter.correlation(avg_corr_coeff,savefig=True)
```



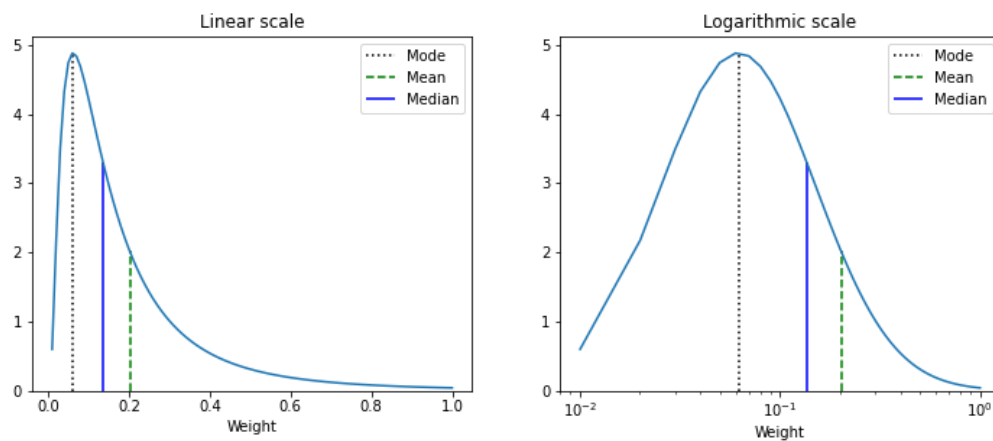
## 2.7.7 Inter spike intervals

```
# Inter spike intervals with exponential curve fit for neuron 1 in the Excitatory pool
Plotter.isi_exponential_fit(E,neuron=1,bin_size=10, savefig=True)
```



### 2.7.8 Linear and Lognormal curve fit of Synaptic weights

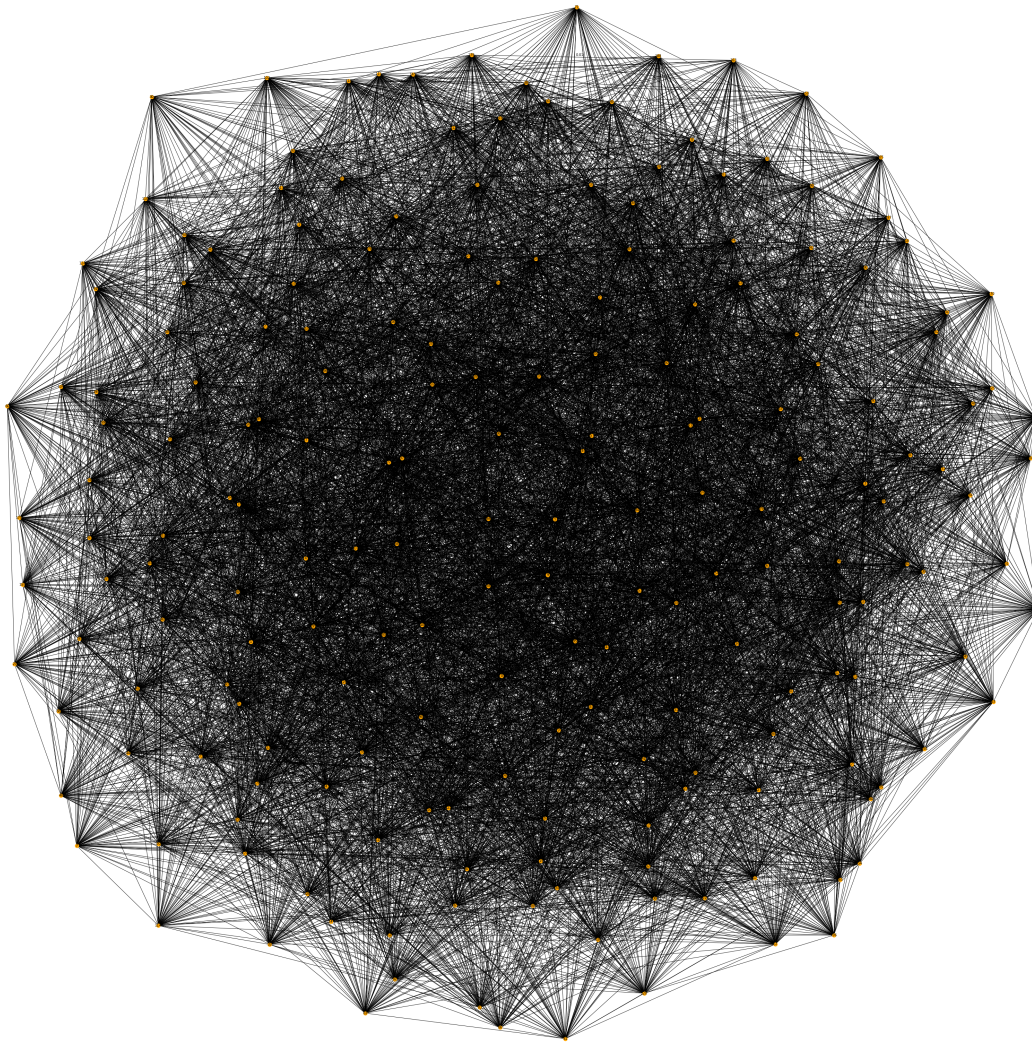
```
# Distribution of connection weights in linear and lognormal scale
Plotter.linear_lognormal_fit(weights=Wee,num_points=100, savefig=True)
```





### 2.7.9 Network plot

```
# Draw network connectivity using the pearson correlation function between neurons in_
↪ the excitatory pool
Plotter.plot_network(avg_corr_coeff,corr_thres=0.01,fig_name='network.png')
```





## 2.8 Statistics and Analysis functions

### 2.8.1 t-lagged auto correlation between neural activity

```
from sorn import Statistics
pearson_corr_matrix = Statistics.autocorr(firing_rates = [1,1,5,6,3,7], t= 2)
```

### 2.8.2 Fano factor

```
# To verify poissonian process in spike generation of neuron 10
mean_firing_rate, variance_firing_rate, fano_factor = Statistics.fanofactor(spike_train=_,
↳E,
                                                                    neuron = 10,
                                                                    window_size = 10)
```

### 2.8.3 Spike Source Entropy

```
# Measure the uncertainty about the origin of spike from the network using entropy
sse = Statistics.spike_source_entropy(spike_train= E, num_neurons=200)
```



## REFERENCE

### 3.1 SORN Network

#### 3.1.1 Sorn

The following methods are available via SORN

**class** sorn.sorn.Sorn

This class wraps initialization of the network and its parameters

**eta\_inhib** = 0.001

**eta\_ip** = 0.01

**eta\_stdp** = 0.004

**static initialize\_activity\_vector**(*ne: int, ni: int*)

Initialize the activity vectors X and Y for excitatory and inhibitory neurons

**Parameters**

- **ne** (*int*) – Number of excitatory neurons
- **ni** (*int*) – Number of inhibitory neurons

**Returns** Array of activity vectors of excitatory population y (array): Array of activity vectors of inhibitory population

**Return type** x (array)

**static initialize\_threshold\_matrix**(*te\_min: float, te\_max: float, ti\_min: float, ti\_max: float*)

Initialize the threshold for excitatory and inhibitory neurons

**Parameters**

- **te\_min** (*float*) – Min threshold value for excitatory units
- **te\_max** (*float*) – Min threshold value for inhibitory units
- **ti\_min** (*float*) – Max threshold value for excitatory units
- **ti\_max** (*float*) – Max threshold value for inhibitory units

**Returns** Threshold values for excitatory units ti (array): Threshold values for inhibitory units

**Return type** te (array)

```
static initialize_weight_matrix(network_type: str, synaptic_connection: str, self_connection: str,
                                lambda_w: int)
```

Wrapper for initializing the weight matrices for SORN

### Parameters

- **network\_type** (*str*) – Sparse or Dense
- **synaptic\_connection** (*str*) – EE, EI, IE. Note that Sparse connection is defined only for EE connections
- **self\_connection** (*str*) – True or False: Synaptic delay or time delay
- **lambda\_w** (*int*) – Average number of incoming and outgoing connections per neuron

**Returns** Array of connection strengths

**Return type** weight\_matrix (array)

```
lambda_ee = 20
```

```
lambda_ei = 40
```

```
lambda_ie = 100
```

```
mu_ip = 0.1
```

```
ne = 200
```

```
network_type_ee = 'Sparse'
```

```
network_type_ei = 'Sparse'
```

```
network_type_ie = 'Dense'
```

```
ni = 40
```

```
nu = 10
```

```
sigma_ip = 0.0
```

```
te_max = 1.0
```

```
te_min = 0.0
```

```
ti_max = 0.5
```

```
ti_min = 0.0
```

### 3.1.2 Plasticity

The following methods are available via Plasticity

```
class sorn.sorn.Plasticity
```

Instance of class Sorn. Inherits the variables and functions defined in class Sorn. It encapsulates all plasticity mechanisms mentioned in the article. Inherits all attributed from parent class Sorn

**static initialize\_plasticity()**

Initialize weight matrices for plasticity phase based on network configuration

**Parameters** **kwargs** (*self.\_\_dict\_\_*) – All arguments are inherited from Sorn attributes

**Returns** Weight matrices WEI, WEE, WIE and threshold matrices Te, Ti and Initial state vectors X,Y

**Return type** tuple(array)

**ip**(*te: numpy.array, x: numpy.array*)

Intrinsic Plasticity mechanism :param te: Threshold vector of excitatory units :type te: array :param x: Excitatory network activity :type x: array

**Returns** Threshold vector of excitatory units

**Return type** te (array)

**istdp**(*wei: numpy.array, x: numpy.array, y: numpy.array, cutoff\_weights: list*)

Apply iSTDP rule, which regulates synaptic strength between the pre inhibitory(Xj) and post Excitatory(Xi) synaptic neurons :param wei: Synaptic strengths from inhibitory to excitatory :type wei: array :param x: Excitatory network activity :type x: array :param y: Inhibitory network activity :type y: array :param cutoff\_weights: Maximum and minimum weight ranges :type cutoff\_weights: list

**Returns** Synaptic strengths from inhibitory to excitatory

**Return type** wei (array)

**static ss**(*wee: numpy.array*)

Synaptic Scaling or Synaptic Normalization :param wee: Weight matrix :type wee: array

**Returns** Scaled Weight matrix

**Return type** wee (array)

**stdp**(*wee: numpy.array, x: numpy.array, cutoff\_weights: list*)

Apply STDP rule : Regulates synaptic strength between the pre(Xj) and post(Xi) synaptic neurons :param wee: Weight matrix :type wee: array :param x: Excitatory network activity :type x: array :param cutoff\_weights: Maximum and minimum weight ranges :type cutoff\_weights: list

**Returns** Weight matrix

**Return type** wee (array)

**static structural\_plasticity**(*wee: numpy.array*)

Add new connection value to the smallest weight between excitatory units randomly :param wee: Weight matrix :type wee: array

**Returns** Weight matrix

**Return type** wee (array)

### 3.1.3 MatrixCollection

The following methods are available via `MatrixCollection`

**class** `sorn.sorn.MatrixCollection`(*phase: str, state: Optional[dict] = None*)

Collect all matrices initialized and updated during simulation(plasiticity and training phases)

**Parameters**

- **phase** (*str*) – Training or Plasticity phase
- **state** (*dict*) – Network activity, threshold and connection matrices

**Returns** `MatrixCollection` instance

**network\_activity\_t**(*excitatory\_net: numpy.array, inhibitory\_net: numpy.array, i: int*)

Network state at current time step

**Parameters**

- **excitatory\_net** (*array*) – Excitatory network activity
- **inhibitory\_net** (*array*) – Inhibitory network activity
- **i** (*int*) – Time step

**Returns** Updated Excitatory and Inhibitory states

**Return type** `tuple(array)`

**network\_activity\_t\_1**(*x: numpy.array, y: numpy.array, i: int*)

Network activity at previous time step

**Parameters**

- **x** (*array*) – Excitatory network activity
- **y** (*array*) – Inhibitory network activity
- **i** (*int*) – Time step

**Returns** Previous Excitatory and Inhibitory states

**Return type** `tuple(array)`

**threshold\_matrix**(*te: numpy.array, ti: numpy.array, i: int*)

Update threshold matrices

**Parameters**

- **te** (*array*) – Excitatory threshold
- **ti** (*array*) – Inhibitory threshold
- **i** (*int*) – Time step

**Returns** Threshold Matrices `Te` and `Ti`

**Return type** `tuple(array)`

**weight\_matrix**(*wee: numpy.array, wei: numpy.array, wie: numpy.array, i: int*)

Update weight matrices

**Parameters**

- **wee** (*array*) – Excitatory-Excitatory weight matrix
- **wei** (*array*) – Inhibitory-Excitatory weight matrix

- **wie** (*array*) – Excitatory-Inhibitory weight matrix
- **i** (*int*) – Time step

**Returns** Weight Matrices Wee, Wei, Wie

**Return type** tuple(array)

### 3.1.4 NetworkState

The following methods are available via **NetworkState**

**class** sorn.sorn.**NetworkState**(*v\_t: numpy.array*)

The evolution of network states

**Parameters** **v\_t** (*array*) – External input/stimuli

**Returns** NetworkState instance

**Return type** instance(object)

**excitatory\_network\_state**(*wee: numpy.array, wei: numpy.array, te: numpy.array, x: numpy.array, y: numpy.array, white\_noise\_e: numpy.array*)

Activity of Excitatory neurons in the network

**Parameters**

- **wee** (*array*) – Excitatory-Excitatory weight matrix
- **wei** (*array*) – Inhibitory-Excitatory weight matrix
- **te** (*array*) – Excitatory threshold
- **x** (*array*) – Excitatory network activity
- **y** (*array*) – Inhibitory network activity
- **white\_noise\_e** (*array*) – Gaussian noise

**Returns** Current Excitatory network activity

**Return type** x(array)

**incoming\_drive**(*weights: numpy.array, activity\_vector: numpy.array*)

Excitatory Post synaptic potential towards neurons in the reservoir in the absence of external input

**Parameters**

- **weights** (*array*) – Synaptic strengths
- **activity\_vector** (*list*) – Activity of inhibitory or Excitatory neurons

**Returns** Excitatory Post synaptic potential towards neurons

**Return type** incoming(array)

**inhibitory\_network\_state**(*wie: numpy.array, ti: numpy.array, y: numpy.array, white\_noise\_i: numpy.array*)

Activity of Inhibitory neurons in the network

**Parameters**

- **wee** (*array*) – Excitatory-Excitatory weight matrix
- **wie** (*array*) – Excitatory-Inhibitory weight matrix

- **ti** (*array*) – Inhibitory threshold
- **y** (*array*) – Inhibitory network activity
- **white\_noise\_i** (*array*) – Gaussian noise

**Returns** Current Inhibitory network activity

**Return type** *y*(*array*)

**recurrent\_drive**(*wee: numpy.array, wei: numpy.array, te: numpy.array, x: numpy.array, y: numpy.array, white\_noise\_e: numpy.array*)

Network state due to recurrent drive received by the each unit at time  $t+1$ . Activity of Excitatory neurons without external stimuli

**Parameters**

- **wee** (*array*) – Excitatory-Excitatory weight matrix
- **wei** (*array*) – Inhibitory-Excitatory weight matrix
- **te** (*array*) – Excitatory threshold
- **x** (*array*) – Excitatory network activity
- **y** (*array*) – Inhibitory network activity
- **white\_noise\_e** (*array*) – Gaussian noise

**Returns** Recurrent network state

**Return type** *xt*(*array*)

### 3.1.5 Simulator

The following methods are available via `Simulator_`

**class** `sorn.sorn.Simulator_`

Simulate SORN using external input/noise using the fresh or pretrained matrices

**Parameters**

- **inputs** (*np.array, optional*) – External stimuli. Defaults to None.
- **phase** (*str, optional*) – Plasticity phase. Defaults to “plasticity”.
- **matrices** (*dict, optional*) – Network states, connections and threshold matrices. Defaults to None.
- **timesteps** (*int, optional*) – Total number of time steps to simulate the network. Defaults to 1.
- **noise** (*bool, optional*) – If True, noise will be added. Defaults to True.

**Returns**

Network states, connections and threshold matrices

*X\_all*(*array*): Excitatory network activity collected during entire simulation steps

*Y\_all*(*array*): Inhibitory network activity collected during entire simulation steps

*R\_all*(*array*): Recurrent network activity collected during entire simulation steps

*frac\_pos\_active\_conn*(*list*): Number of positive connection strengths in the network at each time step during simulation



**Return type** last\_state(dict)

**run**(inputs: Optional[numpy.array] = None, phase: str = 'plasticity', state: Optional[dict] = None, timesteps: Optional[int] = None, noise: bool = True, freeze: Optional[list] = None, callbacks: list = [], \*\*kwargs)

Simulation/Plasticity phase

#### Parameters

- **inputs** (np.array, optional) – External stimuli. Defaults to None.
- **phase** (str, optional) – Plasticity phase. Defaults to “plasticity”
- **state** (dict, optional) – Network states, connections and threshold matrices. Defaults to None.
- **timesteps** (int, optional) – Total number of time steps to simulate the network. Defaults to 1.
- **noise** (bool, optional) – If True, noise will be added. Defaults to True.
- **freeze** (list, optional) – List of synaptic plasticity mechanisms which will be turned off during simulation. Defaults to None.
- **callbacks** (list, optional) – Requested values from [“ExcitatoryActivation”, “InhibitoryActivation”, “RecurrentActivation”, “WEE”, “WEI”, “TE”, “EEConnection-Counts”] collected and returned from the simulate sorn object.

#### Returns

Network states, connections and threshold matrices

callback\_values(dict): Requested network parameters and activations

**Return type** last\_state(dict)

**update\_callback\_state**(\*args) → None

### 3.1.6 Trainer

The following methods are available via Trainer\_

**class sorn.sorn.Trainer\_**

Train the network with the fresh or pretrained network matrices and external stimuli

**run**(inputs: Optional[numpy.array] = None, phase: str = 'training', state: Optional[dict] = None, timesteps: Optional[int] = None, noise: bool = True, freeze: Optional[list] = None, callbacks: list = [], \*\*kwargs)

Train the network with the fresh or pretrained network matrices and external stimuli

Args: inputs(np.array, optional): External stimuli. Defaults to None.

phase(str, optional): Training phase. Defaults to “training”.

state(dict, optional): Network states, connections and threshold matrices. Defaults to None.

timesteps(int, optional): Total number of time steps to simulate the network. Defaults to 1.

noise(bool, optional): If True, noise will be added. Defaults to True.

freeze(list, optional): List of synaptic plasticity mechanisms which will be turned off during simulation. Defaults to None.

max\_workers(int, optional): Maximum workers for multithreading the plasticity steps

### Returns

Network states, connections and threshold matrices

X\_all(array): Excitatory network activity collected during entire simulation steps

Y\_all(array): Inhibitory network activity collected during entire simulation steps

R\_all(array): Recurrent network activity collected during entire simulation steps

frac\_pos\_active\_conn(list): Number of positive connection strengths in the network at each time step during simulation

**Return type** last\_state(dict)

**update\_callback\_state**(\*args) → None

## 3.2 Utility Functions

### 3.2.1 Plotting

The following methods are available via `Plotter`

**class** sorn.utils.Plotter

Wrapper class to call plotting methods

**static correlation**(corr: numpy.array, savefig: bool)

Plot correlation between neurons

#### Parameters

- **corr** (array) – Correlation matrix
- **savefig** (bool) – If true will save the plot at the current working directory

**Returns** Neuron Correlation plot

**Return type** matplotlib.pyplot

**static hamming\_distance**(hamming\_dist: list, savefig: bool)

Hamming distance between true networks states and perturbed network states

#### Parameters

- **hamming\_dist** (list) – Hamming distance values
- **savefig** (bool) – If True, save the fig at current working directory

**Returns** Hamming distance between true and perturbed network states

**Return type** matplotlib.pyplot

**static hist\_firing\_rate\_network**(spike\_train: numpy.array, bin\_size: int, savefig: bool)

Plot the histogram of firing rate (total number of neurons spike at each time step)

#### Parameters

- **spike\_train** (array) – Array of spike trains
- **bin\_size** (int) – Histogram bin size
- **savefig** (bool) – If True, plot will be saved in the cwd

**Returns** plot object

**static hist\_incoming\_conn**(*weights: numpy.array, bin\_size: int, histtype: str, savefig: bool*)

Plot the histogram of number of presynaptic connections per neuron

**Parameters**

- **weights** (*array*) – Connection weights
- **bin\_size** (*int*) – Histogram bin size
- **histtype** (*str*) – Same as histtype matplotlib
- **savefig** (*bool*) – If True plot will be saved as png file in the cwd

**Returns** plot object

**Return type** plot (matplotlib.pyplot)

**static hist\_outgoing\_conn**(*weights: numpy.array, bin\_size: int, histtype: str, savefig: bool*)

Plot the histogram of number of incoming connections per neuron

**Parameters**

- **weights** (*array*) – Connection weights
- **bin\_size** (*int*) – Histogram bin size
- **histtype** (*str*) – Same as histtype matplotlib
- **savefig** (*bool*) – If True plot will be saved as png file in the cwd

**Returns** plot object

**static isi\_exponential\_fit**(*spike\_train: numpy.array, neuron: int, bin\_size: int, savefig: bool*)

Plot Exponential fit on the inter-spike intervals during training or simulation phase

**Parameters**

- **spike\_train** (*array*) – Array of spike trains
- **neuron** (*int*) – Target neuron
- **bin\_size** (*int*) – Spike train will be splitted into bins of size bin\_size
- **savefig** (*bool*) – If True, plot will be saved in the cwd

**Returns** plot object

**static linear\_lognormal\_fit**(*weights: numpy.array, num\_points: int, savefig: bool*)

Lognormal curve fit on connection weight distribution

**Parameters**

- **weights** (*array*) – Connection weights
- **num\_points** (*int*) – Number of points to be plotted in the x axis
- **savefig** (*bool*) – If True, plot will be saved in the cwd

**Returns** plot object

**static network\_connection\_dynamics**(*connection\_counts: numpy.array, savefig: bool*)

Plot number of positive connection in the excitatory pool

**Parameters**

- **connection\_counts** (*array*) –
- **savefig** (*bool*) –

**Returns** plot object

**static plot\_network**(*corr: numpy.array, corr\_thres: float, fig\_name: Optional[str] = None*)

Network x graphical visualization of the network using the correlation matrix

**Parameters**

- **corr** (*array*) – Correlation between neurons
- **corr\_thres** (*array*) – Threshold to prune the connection. Smaller the threshold, higher the density of connections
- **fig\_name** (*array, optional*) – Name of the figure. Defaults to None.

**Returns** Plot instance

**Return type** matplotlib.pyplot

**static raster\_plot**(*spike\_train: numpy.array, savefig: bool*)

Raster plot of spike trains

**Parameters**

- **spike\_train** (*array*) – Array of spike trains
- **with\_firing\_rates** (*bool*) – If True, firing rate of the network will be plotted
- **savefig** (*bool*) – If True, plot will be saved in the cwd

**Returns** plot object

**static scatter\_plot**(*spike\_train: numpy.array, savefig: bool*)

Scatter plot of spike trains

**Parameters**

- **spike\_train** (*list*) – Array of spike trains
- **with\_firing\_rates** (*bool*) – If True, firing rate of the network will be plotted
- **savefig** (*bool*) – If True, plot will be saved in the cwd

**Returns** plot object

**static weight\_distribution**(*weights: numpy.array, bin\_size: int, savefig: bool*)

Plot the distribution of synaptic weights

**Parameters**

- **weights** (*array*) – Connection weights
- **bin\_size** (*int*) – Spike train will be splited into bins of size bin\_size
- **savefig** (*bool*) – If True, plot will be saved in the cwd

**Returns** plot object

### 3.2.2 Statistics and Analysis

The following methods are available via `Statistics`

**class** `sorn.utils.Statistics`

Wrapper class for statistical analysis methods

**static** `autocorr(firing_rates: list, t: int = 2)`

Score interpretation - scores near 1 imply a smoothly varying series - scores near 0 imply that there's no overall linear relationship between a data point and the following one (that is, `plot(x[-length(x)],x[-1])` won't give a scatter plot with any apparent linearity)

- scores near -1 suggest that the series is jagged in a particular way: if one point is above the mean, the next is likely to be below the mean by about the same amount, and vice versa.

**Parameters**

- **firing\_rates** (*list*) – Firing rates of the network
- **t** (*int, optional*) – Window size. Defaults to 2.

**Returns** Autocorrelation between neurons given their firing rates

**Return type** array

**static** `avg_corr_coeff(spike_train: numpy.array)`

Measure Average Pearson correlation coefficient between neurons

**Parameters** **spike\_train** (*array*) – Neural activity

**Returns** Average correlation coefficient

**Return type** array

**static** `fanofactor(spike_train: numpy.array, neuron: int, window_size: int)`

Investigate whether neuronal spike generation is a poisson process

**Parameters**

- **spike\_train** (*np.array*) – Spike train of neurons in the reservoir
- **neuron** (*int*) – Target neuron in the pool
- **window\_size** (*int*) – Sliding window size for time step ranges to be considered for measuring the fanofactor

**Returns** Fano factor of the neuron spike train

**Return type** float

**static** `firing_rate_network(spike_train: numpy.array)`

Calculate number of neurons spikes at each time step. Firing rate of the network

**Parameters** **spike\_train** (*array*) – Array of spike trains

**Returns** firing\_rate

**Return type** int

**static** `firing_rate_neuron(spike_train: numpy.array, neuron: int, bin_size: int)`

Measure spike rate of given neuron during given time window

**Parameters**

- **spike\_train** (*array*) – Array of spike trains

- **neuron** (*int*) – Target neuron in the reservoir
- **bin\_size** (*int*) – Divide the spike trains into bins of size *bin\_size*

**Returns** *firing\_rate*

**Return type** *int*

**static hamming\_distance**(*actual\_spike\_train: numpy.array, perturbed\_spike\_train: numpy.array*)

Hamming distance between true networks states and perturbed network states

**Parameters**

- **actual\_spike\_train** (*np.array*) – True network's states
- **perturbed\_spike\_train** (*np.array*) – Perturbed network's states

**Returns** Hamming distance between true and perturbed network states

**Return type** *float*

**static scale\_dependent\_smoothness\_measure**(*firing\_rates: list*)

Smoothen the firing rate depend on its scale. Smaller values corresponds to smoother series

**Parameters** **firing\_rates** (*list*) – List of number of active neurons per time step

**Returns** Float value signifies the smoothness of the semantic changes in firing rates

**Return type** *sd\_diff* (*list*)

**static scale\_independent\_smoothness\_measure**(*firing\_rates: list*)

Smoothen the firing rate independent of its scale. Smaller values corresponds to smoother series

**Parameters** **firing\_rates** (*list*) – List of number of active neurons per time step

**Returns** Float value signifies the smoothness of the semantic changes in firing rates

**Return type** *coeff\_var* (*list*)

**static spike\_source\_entropy**(*spike\_train: numpy.array, num\_neurons: int*)

Measure the uncertainty about the origin of spike from the network using entropy

**Parameters**

- **spike\_train** (*np.array*) – Spike train of neurons
- **num\_neurons** (*int*) – Number of neurons in the reservoir

**Returns** Spike source entropy of the network

**Return type** *int*

**static spike\_time\_intervals**(*spike\_train*)

Generate spike time intervals *spike\_trains*

**Parameters** **spike\_train** (*array*) – Network activity

**Returns** Inter spike intervals for each neuron in the reservoir

**Return type** *list*

**static spike\_times**(*spike\_train: numpy.array*)

Get the time instants at which neuron spikes

**Parameters** **spike\_train** (*array*) – Spike trains of neurons

**Returns** Spike time of each neurons in the pool

**Return type** (array)





## CONTRIBUTIONS

If you wish to contribute, please

1. Fork the github repo as:

```
git clone git@github.com:your-user-name/sorn.git sorn-yourname
cd sorn-yourname
git remote add upstream git://github.com/saran-nns/sorn.git
```

2. Create a branch as:

```
git checkout -b your_branch_name
```

3. Before pull request, please retrieve the changes from the sorn *master-branch* as:

```
git fetch master
git rebase master
```

and the changes can be discussed there.

If you find a bug in the code or errors in the documentation, please open a new issue in the Github repository and report the bug or the error. Please provide sufficient information for the bug to be reproduced.



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Please cite the package as:

```
@software{saranraj_nambusubramaniyan_2020_4184103,  
author      = {Saranraj Nambusubramaniyan},  
title       = {Saran-nns/sorn: Stable alpha release},  
month       = nov,  
year        = 2020,  
publisher   = {Zenodo},  
version     = {v0.3.1},  
doi         = {10.5281/zenodo.4184103},  
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↪Circuits Solving General Intelligence Tasks at the Imminence of Chaos DOI: 10.13140/RG.  
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